

# Dispersion Optimization in GeO<sub>2</sub>-doped Silica Photonic Crystal Fibers with Circular Lattice

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## ABSTRACT:

In this paper, we analyze the dispersion properties of photonic crystal fiber with the core replaced by a composite of 85% SiO<sub>2</sub>-15% GeO<sub>2</sub>. The air hole's radii of the layers in the cladding are designed differently to improve the dispersion and nonlinear properties of the fibers. Both anomalous and all-normal dispersions have been optimized. Based on numerical simulation results, two optimal structures ( $d_1/\Lambda = 0.4$ ,  $\Lambda = 0.9 \mu\text{m}$  and  $d_1/\Lambda = 0.45$  and  $\Lambda = 1.0 \mu\text{m}$ ) are proposed with a very small dispersion value of 0.298 ps/nm.km and  $-0.311$  ps/nm.km at the pump wavelength of 1.53  $\mu\text{m}$  and 0.985  $\mu\text{m}$ , respectively. The high nonlinear coefficient, small effective mode area, and very low attenuation of about  $10^{-7}$  dB/m at the pump wavelength are also favorable conditions for the application of broad-spectrum supercontinuum with low peak power. The proposed fibers can be new supercontinuum sources that effectively replace glass core fibers.

**KEYWORDS:** Photonic Crystal Fibers, Composite SiO<sub>2</sub>-GeO<sub>2</sub>, Flat Dispersion, Small Effective Mode Area, Low Attenuation.

## 1. INTRODUCTION

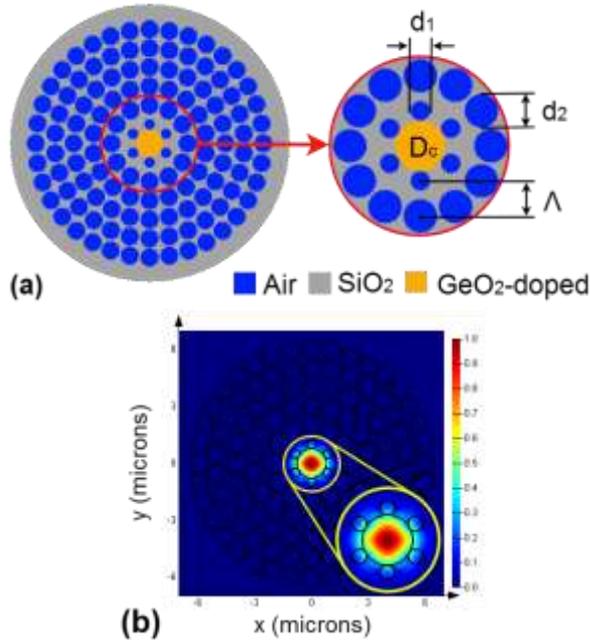
With its excellent nonlinear properties, Photonic Crystal Fiber (PCF) has verified wide applicability in fields including: optical coherence tomography, photonic device testing, optical communications [1]–[5], and optical microscopy [6], [7]. Furthermore, it is also the best nonlinear mediums for supercontinuum (SC) generation [8], due to its flexibility in structural design and high nonlinearity. Generally, silica-based solid-core PCFs are most commonly used to produce a broad SC with high intensity but it is difficult to extend the spectrum further in the mid-infrared region (MIR) due to silica's high matter absorption. To avoid this limitation of silica, many recent studies have suggested the development of broadband sources based on different optical mediums such as the hollow-core photonic crystal fibers which are infiltrated by highly nonlinear liquids [9]–[12], fibers made of fluoride [13]–[16] or chalcogenide [17]–[20]. Although the efficiency of SC spectrum expansion is improved in MIR, they are often expensive, fragile and rather difficult to handle. The physical properties of Germania (GeO<sub>2</sub>) and silica (SiO<sub>2</sub>) are similar but the phonon energy of GeO<sub>2</sub> ( $\sim 820 \text{ cm}^{-1}$ ) is lower than of silica ( $\sim 1100 \text{ cm}^{-1}$ ), its nonlinear refractive index ( $9.5 \times 10^{-20} \text{ m}^2 \cdot \text{W}^{-1}$ ) is about 3.5 times higher than that of silica

( $2.74 \times 10^{-20} \text{ m}^2 \cdot \text{W}^{-1}$ ). [21]. This makes the transmission window of GeO<sub>2</sub>-based PCFs longer in MIR [22]. The high optical transparency of pure GeO<sub>2</sub> and GeO<sub>2</sub> doped silica fibers in the MIR is one of the advantages that attract the attention of the research groups. More, these PCFs have been fabricated in practice by drawing methods for silica fibers [23]. Recently, many publications have presented on SC spectral broadening in MIR based on GeO<sub>2</sub>-doped core silica fibers [22], [23]–[28]. SC spectral expansion using GeO<sub>2</sub>-doped silica fibers with different laser pump pulses at 1.5  $\mu\text{m}$  and 2  $\mu\text{m}$  have been also investigated in [29], [30]. In the experiment, some silica fibers have a GeO<sub>2</sub> doped core with concentrations varying from 51 mol% to 97 mol% [31]–[33], and low loss (less than 120 dB/km at 1.9–2  $\mu\text{m}$ ) have been reported. A broad spectrum from 700nm to 3200nm based on GeO<sub>2</sub>-doped PCF at 1.55m pump wavelength was proved by the experiment in the work [34]. The papers [35, 36] showed that GeO<sub>2</sub>-doped PCFs had been experimentally fabricated to obtain broad-spectrum SC at different pumping wavelengths although the damage threshold of GeO<sub>2</sub> is low (few orders of magnitude lower than that of silica) [37].

In this paper, we investigate in detail the specific quantities for dispersion and nonlinear properties of

silica fibers doped GeO<sub>2</sub> with a concentration of 15% mol. All-normal and anomalous flat dispersions beneficial to SC generation are obtained. More, quantities such as effective mode area, nonlinear coefficient, and attenuation are also analyzed numerically and compared with previous publications on GeO<sub>2</sub>-doped PCFs. Two optimized structures with flat dispersion, high nonlinear coefficient, and low attenuation are proposed to guide SC generation application.

## 2. NUMERICAL MODELLING OF PCFs



**Fig. 1.** Cross-section view of the circular GeO<sub>2</sub>-doped silica PCF (a), and the light confinement in the core of PCF with  $\Lambda = 1.0 \mu\text{m}$ ;  $d_1/\Lambda = 0.45$  (b).

The structure and optical properties of GeO<sub>2</sub>-doped silica PCF were simulated using Lumerical Mode Solution (LMS) software. The full-vector finite-difference eigenmode method is used to mesh waveguide geometry and is capable of fitting arbitrary waveguide structures. Once the structure is meshed, Maxwell's equations are then built into a matrix eigenvalue problem and solved using sparse matrix techniques to calculate the spatial profile and frequency dependence of modes. The boundary condition is the perfectly matched layers with rectangular shape which strongly absorbs the waves coming from the calculated region without any reflection. As a result, we obtain the effective refractive index, loss, and the field intensity profile of the fundamental mode of the PCFs. The cross-sectional structure of GeO<sub>2</sub>-doped silica PCF is shown in Fig. 1a. Six layers of air holes with diameter  $d$  separated by a distance  $\Lambda$  are arranged in a circular pattern around the

core. The works [9]–[11] verified that the dispersion was efficiently controlled by reasonably adjusting the air hole's size of the first layer near the core. Even the Zero Dispersion Wavelengths (ZDWs) shift is strongly affected by this. But the attenuation of the fundamental-mode or the higher order modes is dominated by the size of the remaining layers. From this idea, we modified the lattice structure which focused on the difference between the air hole's diameter of the layers in the cladding to control the dispersion and nonlinear properties of the fibers. The filling factor  $d_1/\Lambda$  varies from 0.3–0.65 ( $d_1$  is the air hole's diameter of the first layer closest to the core) while  $d_2/\Lambda$  is kept constant at 0.95 ( $d_2$  is the air hole's diameter of the second layer and others). The core of the fibers was completely replaced by composite materials 85% SiO<sub>2</sub>-15% GeO<sub>2</sub> with the diameter determined according to the formula  $D_c = 2\Lambda - d_1$ . By skillfully tuning such lattice parameters, PCF has demonstrated good confinement of light in the core (Fig. 1b).

To design the structures of PCFs, first, the parameters of the refractive index of composite materials 85% SiO<sub>2</sub>-15% GeO<sub>2</sub> were calculated according to formula (1–3) [38],[39] and entered into the data system of LMS. Next, the circular lattice is selected from the lattice types data, and the boundary conditions are set up so that the LMS can solve the Maxwell wave equation with minimal loss. The wavelength range investigated is 0.5–2.0  $\mu\text{m}$  which is compatible with existing LMS data.

$$n_{\text{SiO}_2}^2(\lambda) = 1 + \frac{0.6961663\lambda^2}{\lambda^2 - 4.679148 \times 10^{-3}} + \frac{0.4079426\lambda^2}{\lambda^2 - 1.3512063 \times 10^{-2}} + \frac{0.8974794\lambda^2}{\lambda^2 - 97.93400254} \quad (1)$$

$$n_{\text{GeO}_2}^2(\lambda) = 1 + \frac{0.80686642\lambda^2}{\lambda^2 - 4.75722 \times 10^{-3}} + \frac{0.71815848\lambda^2}{\lambda^2 - 2.3705545 \times 10^{-2}} + \frac{0.85416831\lambda^2}{\lambda^2 - 140.2313298} \quad (2)$$

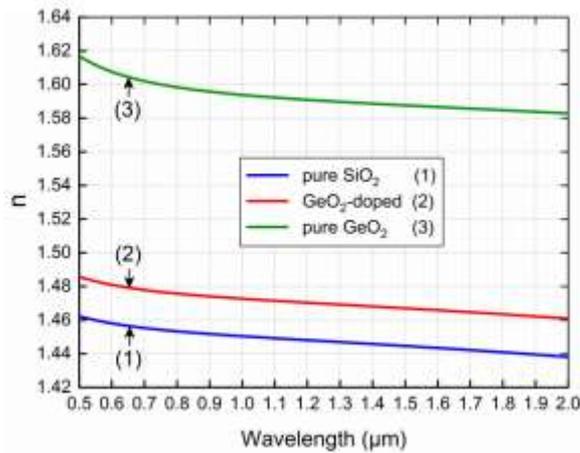
$$n_{(\text{GeO}_2-\text{SiO}_2)}^2(\lambda) = 1 + \sum_{i=1}^3 \frac{[SB_i + X(GB_i - SB_i)]\lambda^2}{\lambda^2 - [SC_i + X(GC_i - SC_i)]^2} \quad (3)$$

Where,  $SB$ ,  $SC$ ,  $GB$ ,  $GC$  are the Sellmeier coefficients for the SiO<sub>2</sub> and GeO<sub>2</sub> glasses, respectively, and  $X$  is the mole fraction of GeO<sub>2</sub> ( $X = 0.15$ ).

**Table 1.** Sellmeier's coefficients for the GeO<sub>2</sub>-doped [39].

Parameters	Values
$B_1$	0.712771318
$B_2$	0.454474982
$B_3$	0.890982737
$C_1$ ( $\mu\text{m}$ )	$6.8489546 \times 10^{-2}$
$C_2$ ( $\mu\text{m}$ )	$1.21900098 \times 10^{-1}$
$C_3$ ( $\mu\text{m}$ )	10.1880265

The dependence of the refractive index of pure SiO<sub>2</sub>, pure GeO<sub>2</sub>, and composite SiO<sub>2</sub>-GeO<sub>2</sub> on wavelength is shown in Fig. 2. Pure GeO<sub>2</sub> has the highest refractive index, but PCFs based on it exhibit a large fiber loss [27], so SiO<sub>2</sub> PCFs with a GeO<sub>2</sub> doped core are a good way to think about minimizing the loss. However, this loss increased as the GeO<sub>2</sub> content increased. Therefore, the GeO<sub>2</sub> doping concentration should also be taken into account when designing the structures of PCFs.

**Fig. 2.** The real parts of the refractive index  $n$  pure SiO<sub>2</sub>, pure GeO<sub>2</sub>, and composite SiO<sub>2</sub>-GeO<sub>2</sub>.

### 3. SIMULATION RESULTS AND ANALYSIS

The higher-order modes have a negligible effect on the spectral expansion in SC applications, so the analysis of the optical properties of the PCFs is only for the fundamental mode. Chromatic dispersion is the phenomenon by which different spectral components of a pulse travel at different velocities, which is characterized by the propagation constant  $\beta$ . Chromatic dispersion includes material dispersion and waveguide

dispersion. The relationship between dispersion ( $D$ ) and effective refractive index of the fiber is described in Equation (4) [40].

$$D = -\frac{\lambda}{c} \frac{\partial^2 \text{Re}[n_{\text{eff}}]}{\partial \lambda^2} \quad (4)$$

Where  $\lambda$  and  $c$  are the wavelength and the speed of light in a vacuum, respectively, and  $\text{Re}[n_{\text{eff}}]$  is the real part of the effective index of the guided mode.

The strongly wavelength-dependent dispersion is dominated by structural parameters such as the lattice constant  $\Lambda$  and the filling factor  $d_1/\Lambda$ . Both all-normal and anomalous dispersions are obtained, shown in Fig. 3. In case  $\Lambda$  is small,  $\Lambda = 0.9 \mu\text{m}$ ;  $1.0 \mu\text{m}$ , dispersion properties are quite diverse including all-normal and anomalous dispersion curves with one or two ZDWs. When  $\Lambda = 0.9 \mu\text{m}$  (Fig. 3a), there are two all-normal dispersion curves with  $d_1/\Lambda = 0.45$  and  $0.5$ . The curve with  $d_1/\Lambda = 0.45$  is closest to the zero-dispersion line in the wavelength range  $0.6\text{--}1.1 \mu\text{m}$ , while the one with  $d_1/\Lambda = 0.5$  is closest to the zero dispersion line in the wavelength range  $1.1\text{--}2.0 \mu\text{m}$ . As  $\Lambda$  increases to  $1.0 \mu\text{m}$  (Fig. 3b), the dispersion with  $d_1/\Lambda = 0.5$  becomes anomalous dispersion with two ZDWs, and  $d_1/\Lambda = 0.45$  is the flattest all-normal dispersion curve and closest to the zero dispersion curve. With  $\Lambda = 1.5 \mu\text{m}$  and  $2.0 \mu\text{m}$  (Fig. 3c and d), the increase of the filling factor  $d_1/\Lambda$  and  $\Lambda$  causes the dispersion curves to shift upwards, beyond the zero dispersion curve. In this case, we achieve anomalous dispersion for all structures. Furthermore, for  $\Lambda = 2.0 \mu\text{m}$ , the increase of the filling factor  $d_1/\Lambda$  increases the value of the dispersion at each defined wavelength.

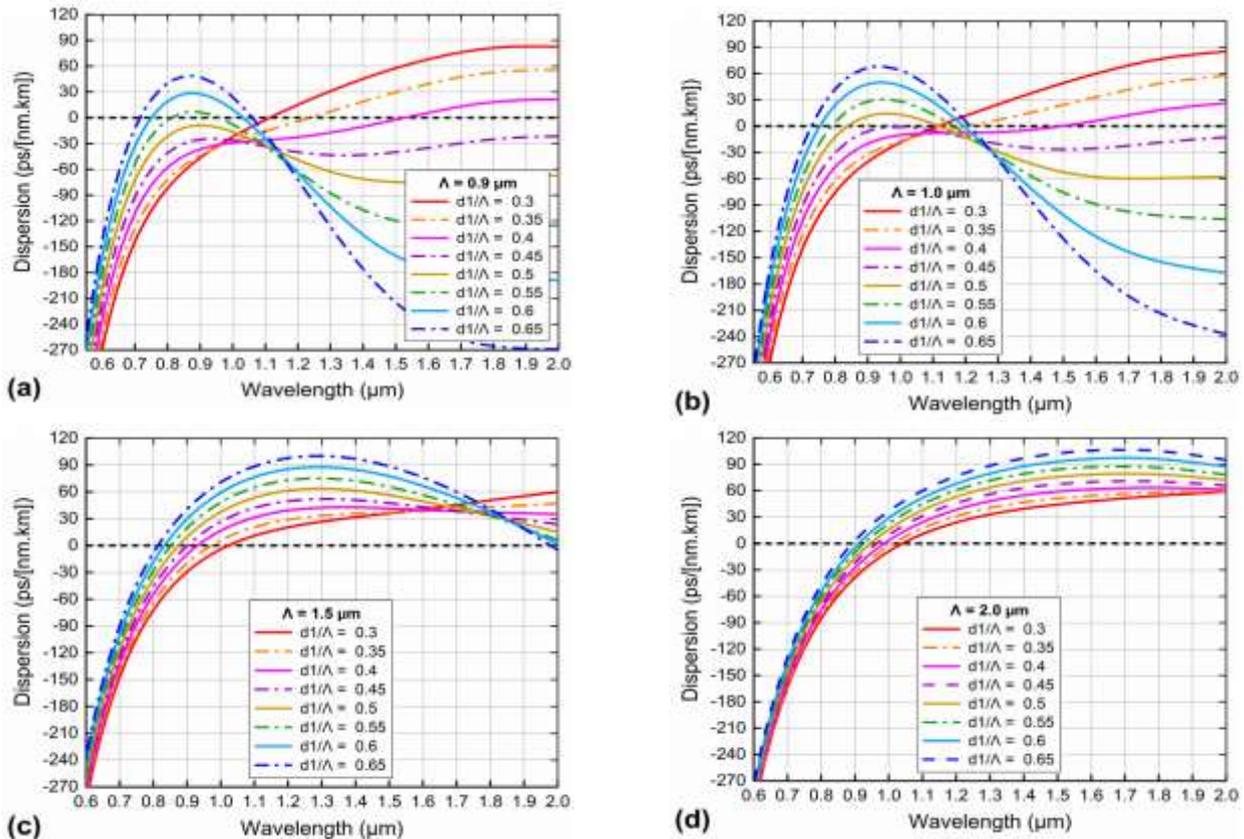
The maximum dispersion value is an essential factor to consider the appropriate pump wavelength in SC generation. Usually, the pump wavelengths are chosen close to the peak of the dispersion curves, which also ensures that the corresponding dispersion values are small enough. The change of dispersion maximum value according to the filling factor with different lattice constants is shown in Fig. 4a. For PCFs with small lattice constants ( $\Lambda = 0.9, 1.0 \mu\text{m}$ ), the peak of the dispersion curves changes strongly. With the filling factors less than  $0.45$ , these values decrease, reaching a minimum at  $d_1/\Lambda = 0.45$  and then increasing when  $d_1/\Lambda$  is greater than  $0.45$ . With larger lattice constants ( $\Lambda = 1.5, 2.0 \mu\text{m}$ ), the dispersion maximum value increases almost linearly with the increase of the filling factors.

**Table 2.** The values of ZDWs of the circular SiO<sub>2</sub>-GeO<sub>2</sub> PCFs.

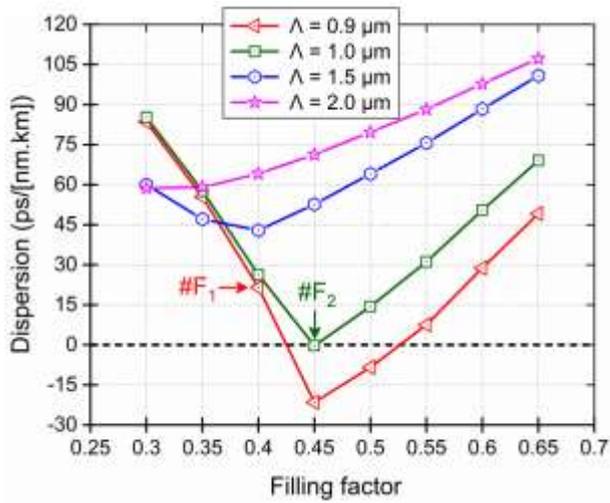
$f = d_1/\Lambda$	$\Lambda = 0.9 \mu\text{m}$		$\Lambda = 1.0 \mu\text{m}$		$\Lambda = 1.5 \mu\text{m}$		$\Lambda = 2.0 \mu\text{m}$
	ZDW <sub>1</sub>	ZDW <sub>2</sub>	ZDW <sub>1</sub>	ZDW <sub>2</sub>	ZDW <sub>1</sub>	ZDW <sub>2</sub>	ZDW <sub>1</sub>
0.3	1.113		1.116		1.022		1.038
0.35	1.237		1.207		0.971		1.011
0.4	1.526		1.498		0.930		0.985
0.45					0.899		0.963
0.5			0.837	1.119	0.874		0.945
0.55	0.810	0.961	0.788	1.164	0.851		0.925
0.6	0.749	1.033	0.752	1.194	0.811		0.910
0.65	0.715	1.060	0.726	1.214	0.813	1.979	0.891

The shift of the ZDWs affects the careful selection of pump wavelengths in the SC generation application, as that relates to the common laser pump wavelengths in practice. Furthermore, the value of dispersion at the pump wavelength must be small enough to improve the SC generation efficiency. Fig. 4b presents the change of ZDWs according to the filling factor  $d_1/\Lambda$  and the values of ZDWs are shown in Tab. 2. For PCFs with

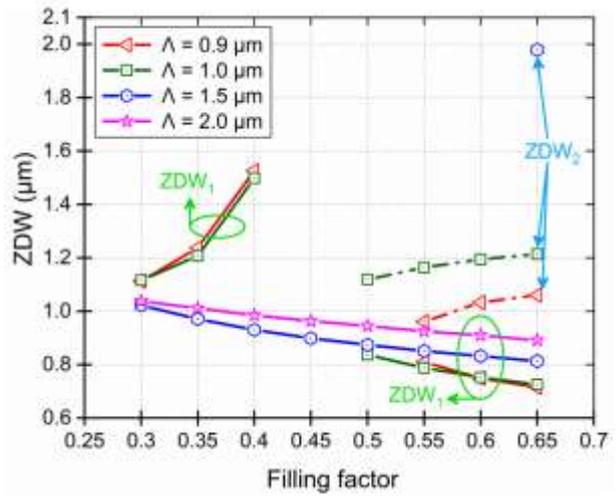
small  $\Lambda$  and  $d_1/\Lambda$ , the ZDW<sub>1</sub> value gradually increases (ZDW<sub>1</sub> of the structure  $\Lambda = 0.9 \mu\text{m}$  and  $d_1/\Lambda = 0.4$  is 1.526), due to the good confinement of light in the small core PCFs. In contrast, ZDW<sub>1</sub> shifts to shorter wavelengths when  $\Lambda$  and  $d_1/\Lambda$  are larger. This suggests that, we can choose the optimal structures with small  $\Lambda$  and  $d_1/\Lambda$  to orient the SC generation application.



**Fig. 3.** The chromatic dispersion characteristics of the circular GeO<sub>2</sub>-doped silica PCF with various values of  $d_1/\Lambda$  and  $\Lambda = 0.9 \mu\text{m}$  (a),  $1.0 \mu\text{m}$  (b),  $1.5 \mu\text{m}$  (c), and  $2.0 \mu\text{m}$  (d).

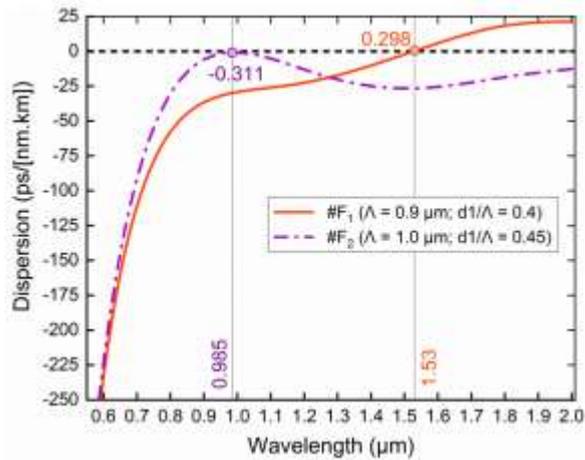


(a) The maximum value of dispersions

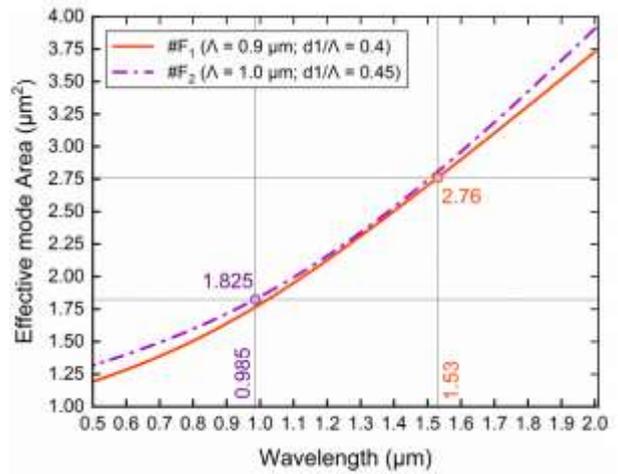


(b) The ZDWs

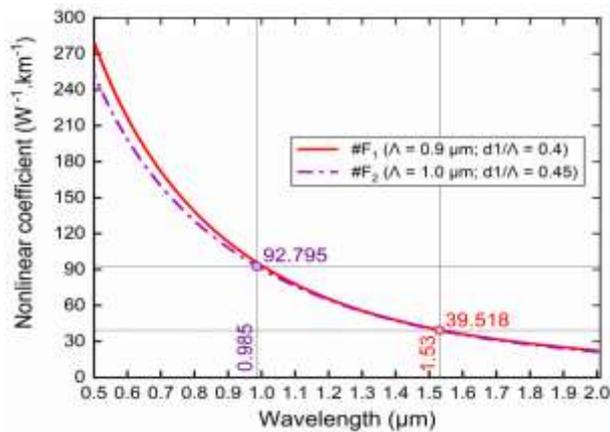
Fig. 4. The maximum value of dispersions and ZDWs with various filling factors  $d1/\Lambda$  and lattice constant  $\Lambda$



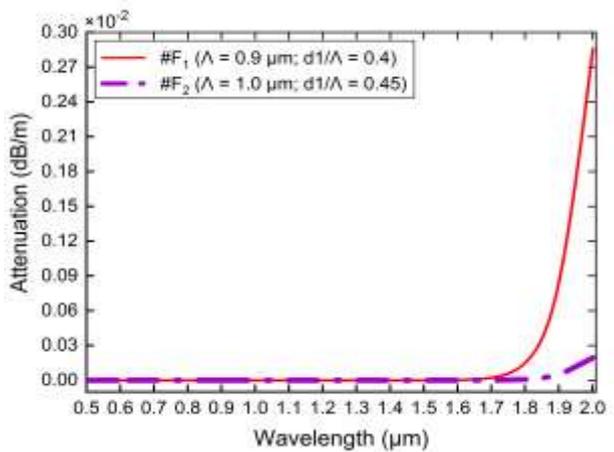
(a) The chromatic dispersion



(b) The effective mode area



(c) The nonlinear coefficient



(d) The attenuation

Fig. 5. The optical characteristics of the fundamental mode for #F<sub>1</sub> and #F<sub>2</sub> fibers.

The appearance of different nonlinear effects in SC generation governs the different properties and broadening of the SC spectrum. This strongly depends on the dispersion properties of the proposed PCFs. The broad SC spectrum, high coherence, and low noise are obtained using fiber with all-normal dispersion. For fibers with anomalous dispersion, or a pump wavelength in the anomalous dispersion regime, the SC spectrum is broader but has lower coherence and higher noise. To diversify the applicability of generating SC suitable for the dispersion regime, we propose two PCFs with all-normal and anomalous flat dispersion, named as #F<sub>1</sub> and #F<sub>2</sub> (Fig. 5a). #F<sub>1</sub> fiber with  $d_1/\Lambda = 0.4$  has the flattest dispersion among anomalous dispersion curves when  $\Lambda = 0.9 \mu\text{m}$ , very small dispersion value of 0.298 ps/nm.km at pump wavelength 1.53  $\mu\text{m}$  (closer to 1.55  $\mu\text{m}$  wavelength of common lasers), is expected to generate a broad and noise SC spectrum with the main mechanism being soliton dynamics. While the #F<sub>2</sub> fiber ( $d_1/\Lambda = 0.45$  and  $\Lambda = 1.0 \mu\text{m}$ ) has normal dispersion with a small dispersion value of  $-0.311$  ps/nm.km at a pump wavelength of 0.985  $\mu\text{m}$  (close to the maximum point of the parabolic dispersion curve) which will give a broad, low noise, and high coherence SC spectrum. Skillfully modifying the structural parameters and choosing a reasonable GeO<sub>2</sub> doping concentration, we obtain a flatter dispersion and the dispersion value at the pump wavelength is smaller than that of the works [25], [28], [42]–[45]. The anomalous dispersion of #F<sub>1</sub> fiber (0.298 ps/nm.km) is about 115 times smaller than the work [44]. Meanwhile, the all-normal dispersion value of #F<sub>2</sub> fiber ( $-0.311$  ps/nm.km) is about 1.8 times, 17 times, and 38 times smaller than the works [25], [32], [43] respectively, but this value is similar to work [28], [41].

Other nonlinear quantities such as effective mode area, nonlinear coefficient, and attenuation of two

fibers #F<sub>1</sub> and #F<sub>2</sub> are also investigated in detail. The effective mode area ( $A_{\text{eff}}$ ) is inversely proportional to the nonlinear coefficient ( $\gamma$ ) according to the formula (5) [45].

$$\gamma(\lambda) = 2\pi \frac{n_2}{\lambda A_{\text{eff}}} \quad (5)$$

Where  $n_2$  is the nonlinear index of the composite (GeO<sub>2</sub>-SiO<sub>2</sub>).

The dependence of the nonlinear coefficient and effective mode area on the step and structure parameters  $d_1/\Lambda$ ,  $\Lambda$  is illustrated in Fig. 5b and c. The increasing wavelength increases the value of  $A_{\text{eff}}$ , which is consistent with the leakage phenomena of modes out of the core into the cladding of PCFs in the long wavelength region. The  $A_{\text{eff}}$  of #F<sub>2</sub> fiber is larger than #F<sub>1</sub> in the investigated wavelength range. The large core also increases the leakage of modes resulting in a larger effective mode area. The values of  $A_{\text{eff}}$  obtained at the pumping wavelength of #F<sub>1</sub> and #F<sub>2</sub> fibers are 2.76  $\mu\text{m}^2$  and 1.825  $\mu\text{m}^2$ , respectively, which are smaller than [28], [29]. We also achieved a high nonlinear coefficient of 39.518  $\text{W}^{-1}.\text{km}^{-1}$  and 92.795  $\text{W}^{-1}.\text{km}^{-1}$  with two fibers #F<sub>1</sub> and #F<sub>2</sub>, respectively, which is an advantage in choosing laser pump sources with medium and small peak power. Especially, very low attenuation values ( $L_k$ ) of about  $10^{-8}$  dB/m of the two proposed fibers are found in the investigated wavelength region, displayed in Fig. 5d. Although the attenuation of both fibers increases sharply at 1.7  $\mu\text{m}$ , it does not affect the SC generation efficiency much because the pump wavelengths of both fibers are lower. Fiber #F<sub>1</sub> has an attenuation value of  $3.681 \times 10^{-7}$  dB/m much larger than fiber #F<sub>2</sub> which is  $4.256 \times 10^{-18}$  dB/m. The structural parameters and values of the proposed two-fiber characteristic quantities are compared with some previous publications on GeO<sub>2</sub>-doped silica PCF, manifested in Table 3.

**Table 3.** The structure parameters and the characteristic quantities of #F<sub>1</sub> and #F<sub>2</sub> fibers at the pump wavelength compared with previous publications on GeO<sub>2</sub>-doped silica PCF.

#	% mol GeO <sub>2</sub>	$D_c$ ( $\mu\text{m}$ )	$\Lambda$ ( $\mu\text{m}$ )	$d_1/\Lambda$	Pump wavelength ( $\mu\text{m}$ )	$A_{\text{eff}}$ ( $\mu\text{m}^2$ )	$\gamma$ ( $\text{W}^{-1}.\text{km}^{-1}$ )	$D$ (ps/nm.km)	$L_k$ (dB/m)
#F <sub>1</sub>	15	1.44	0.9	0.4	1.53	2.76	39.518	0.298	$3.681 \times 10^{-7}$
#F <sub>2</sub>	15	1.55	1.0	0.45	0.985	1.825	92.795	$-0.311$	$4.256 \times 10^{-18}$
[25]	30	-	-	-	1.56	-	-	$-5.5$	-
	40	-	-	-	1.56	-	-	5	-
[28]	61.8	-	-	-	1.55	3.08	108	$-0.322$	$2.6 \times 10^{-5}$
[41]	30	2.8	-	-	1.57	-	11.8	$-0.3$	0.002
[42]	28.66	-	-	-	1.55	1.96	-	$-0.553$	$0.2 \times 10^{-3}$

[43]	4.1	-	-	-	1.55	6.555	13.6	-1.86	-
	7.0	-	-	-	1.55	6.471	14.9	-9.5	-
	13.5	-	-	-	1.55	6.317	16.6	-11.8	-
[44]	-	-	-	-	1.40	7.0	90	34.3	$1.12 \times 10^{-10}$

#### 4. CONCLUSION

Circular lattice PCFs based on  $\text{SiO}_2\text{-GeO}_2$  composite (15% mol concentration of  $\text{GeO}_2$ ) are designed with differences in the air hole radius of the layers in the cladding. The modification of lattice parameters including lattice constant and filling factor helps to optimize the dispersion and nonlinear properties of PCFs. We obtain both all-normal and anomalous flat dispersion. Two proposed structures are suitable for SC generation based on a detailed analysis of numerical simulation results. The dispersion values as small as 0.298 ps/nm.km at pump wavelength 1.53  $\mu\text{m}$  are found for fibers  $d_1/\Lambda = 0.4$  and  $\Lambda = 0.9 \mu\text{m}$  with anomalous dispersion. This fiber also shows a nonlinear coefficient as high as  $39.518 \text{ W}^{-1}.\text{km}^{-1}$ , and attenuation as low as  $3.681 \times 10^{-7} \text{ dB/m}$ , which is expected to generate a broad-spectrum SC with soliton dynamics. All-normal dispersion of fibers  $d_1/\Lambda = 0.45$  and  $\Lambda = 1.0 \mu\text{m}$  will produce a highly coherent broad SC spectrum due to the small value of  $-0.311 \text{ ps/nm.km}$  at a pump wavelength of 0.985  $\mu\text{m}$ . With a higher  $92.795 \text{ W}^{-1}.\text{km}^{-1}$  of nonlinear coefficient and a lower of  $4.256 \times 10^{-18} \text{ dB/m}$  attenuation, this fiber will be suitable for SC generation with small peak power. Two proposed fibers can be a new laser source with low peak power replacing glass core fibers.

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